



兰州 2012超重核合成与性质研讨会



Investigation of rotational properties in superheavy Nobelium isotopes

Wang HuaLei (王华磊)

School of Physics, Zhengzhou University

10-13 August, 2012

Introduction
Theoretical method
Results and...
Summary

Home Page

Title Page



Page 1 of 19

Go Back

Full Screen

Close

Quit



Outline



Introduction



Theoretical Method



Results and Discussions



Summary

Introduction
Theoretical method
Results and...
Summary

[Home Page](#)

[Title Page](#)



Page 2 of 19

[Go Back](#)

[Full Screen](#)

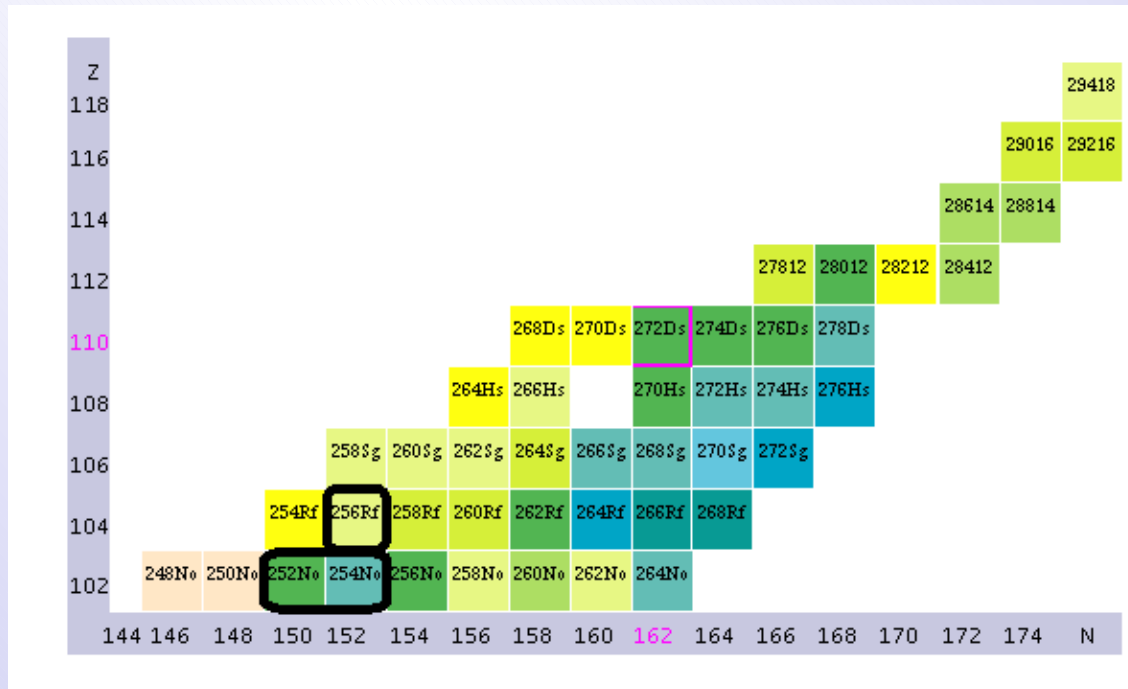
[Close](#)

[Quit](#)



1. Introduction

1.1. Status of synthesis of superheavy nuclei with $Z > 100$



From <http://www.nndc.bnl.gov/chart/>

Introduction

Theoretical method

Results and...

Summary

Home Page

Title Page

◀ ▶

◀ ▶

Page 3 of 19

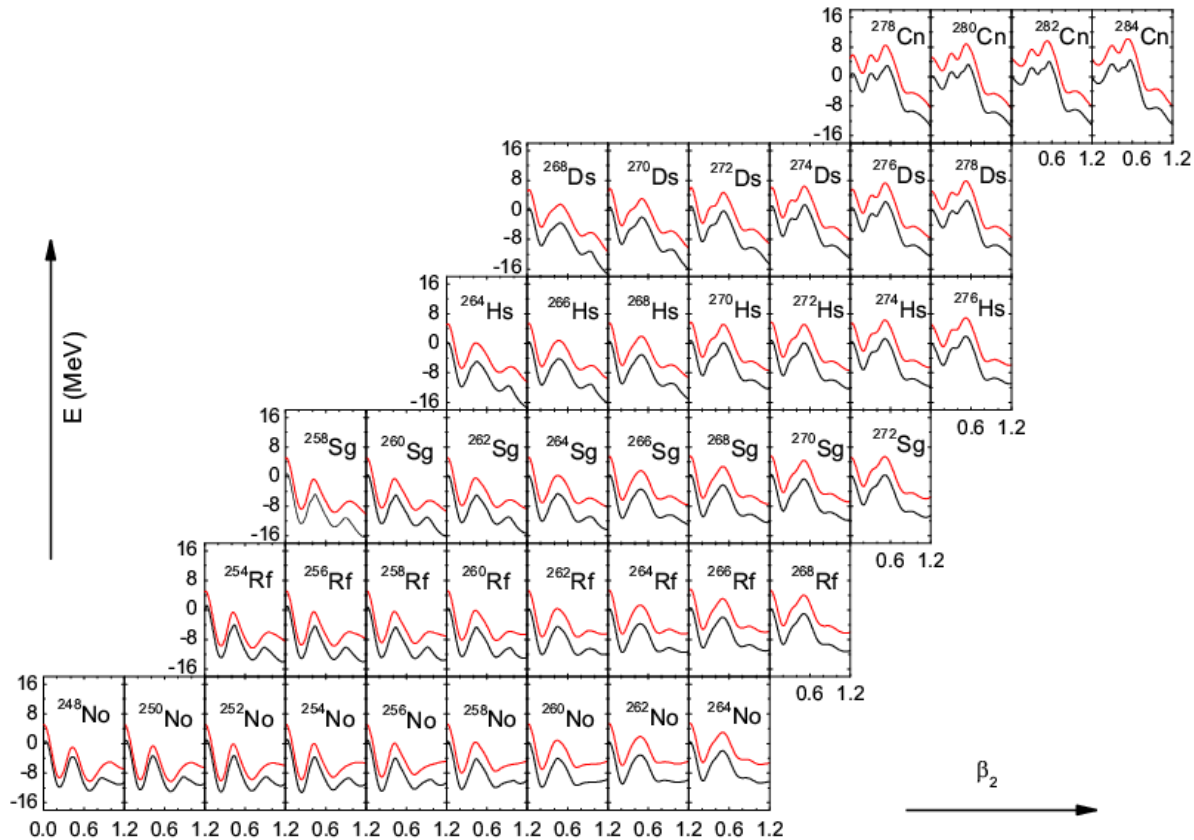
Go Back

Full Screen

Close

Quit

Octupole correlation effects of superheavy nuclei with $100 < Z < 114$



♣ There are no octupole-correlation effects at the normal deformed minima.

H.L Wang et al., Chin. Sci. Bull,57:1761,2012.

Introduction
Theoretical method
Results and ...
Summary

Home Page

Title Page

◀ ▶

◀ ▶

Page 4 of 19

Go Back

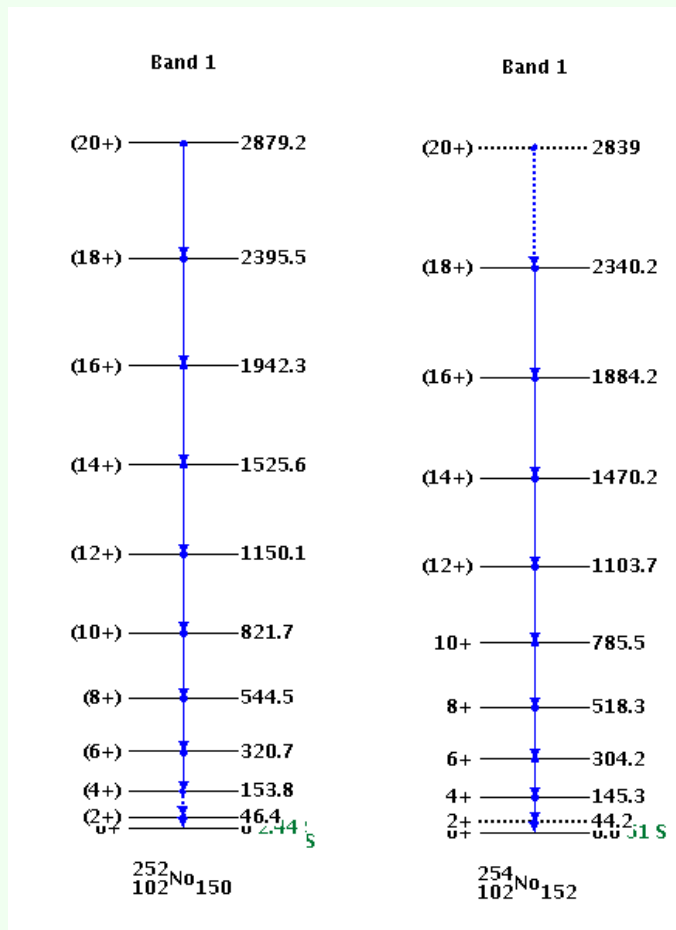
Full Screen

Close

Quit

1.2. High-spin structure of superheavy nuclei

The high-spin level schemes have been constructed in $^{252,254}\text{No}$ and ^{256}Rf .



Refs: R.D.Herzberg et al., PRC65,014303(2001);S.Eeckhaudt et al., EPJA26,227(2005);P.T.Greenlees et al.,PRL 109,012501(2012).



Introduction

Theoretical method

Results and...

Summary

Home Page

Title Page

◀ ▶

◀ ▶

Page 5 of 19

Go Back

Full Screen

Close

Quit



Introduction

Theoretical method

Results and...

Summary

Home Page

Title Page

◀ ▶

◀ ▶

Page 6 of 19

Go Back

Full Screen

Close

Quit

2. Theoretical method

Refs: Phys. Lett. B **435**, 257 (1998); Nucl. Phys. A **578**, 45 (1994); Nucl. Phys. A **536**, 20 (1992); Nucl. Phys. A **81**, 1 (1966); Nucl. Phys. A **669**, 119 (2000); Nucl. Phys. A **435**, 397 (1985); Phys. Rev. C **83**, 011303 (2011).

2.1. The Hamiltonian

The cranking Hamiltonian

$$\hat{H}_\omega = \hat{H}_{WS} + \hat{H}_{pair} - \lambda_1 \hat{N} - \lambda_2 \hat{N}^2 - \omega \hat{j}_x \quad (1)$$

2.2. Total-Routhian-surface Method

Single-particle potential

$$H_{WS} = T + V(r, \hat{\beta}) + V_{l.s}(r, \hat{\beta}) + \frac{1}{2}(1 + \tau_3)V_c(r, \hat{\beta}) \quad (2)$$



§ Lipkin-Nogami pairing

$$E_{LN} = \sum_{j=1}^S e_{k_j} + \sum_{k \neq k_j} 2v_k^2 e_k - \frac{\Delta^2}{G} - G \sum_{k \neq k_j} v_k^4 + G \frac{N-S}{2} - 4\lambda_2 \sum_{k \neq k_j} (u_k v_k)^2 \quad (3)$$

§ Strutinsky shell correction

$$\delta E_{shell} = E_{LN} - \tilde{E}_{Strut.} \quad (4)$$

§ Hartree-Fock-Bogoliubov-Cranking equation

$$\begin{aligned} \sum_{\beta > 0} \left\{ \left[(e_\alpha - \lambda) \delta_{\alpha\beta} - \omega(j_x)_{\alpha\beta} - G \rho_{\bar{\alpha}\bar{\beta}}^* + 4\lambda_2 \rho_{\alpha\beta} \right] U_{\beta\kappa} - \Delta \delta_{\alpha\beta} V_{\bar{\beta}\kappa} \right\} &= E_\kappa U_{\alpha\kappa} \\ \sum_{\beta > 0} \left\{ \left[(e_\alpha - \lambda) \delta_{\alpha\beta} + \omega(j_x)_{\alpha\beta} - G \rho_{\alpha\beta} + 4\lambda_2 \rho_{\bar{\alpha}\bar{\beta}}^* \right] V_{\bar{\beta}\kappa} + \Delta^* \delta_{\alpha\beta} U_{\beta\kappa} \right\} &= E_\kappa V_{\bar{\alpha}\kappa} \end{aligned} \quad (5)$$

§ Macroscopic liquid drop energy

$$E_{LDM}(N, Z, \tilde{\beta}) = \{ [B_s(\tilde{\beta}) - 1] + 2\chi [B_c(\tilde{\beta}) - 1] \} E_s^{(0)} \quad (6)$$

Home Page

Title Page



Page 7 of 19

Go Back

Full Screen

Close

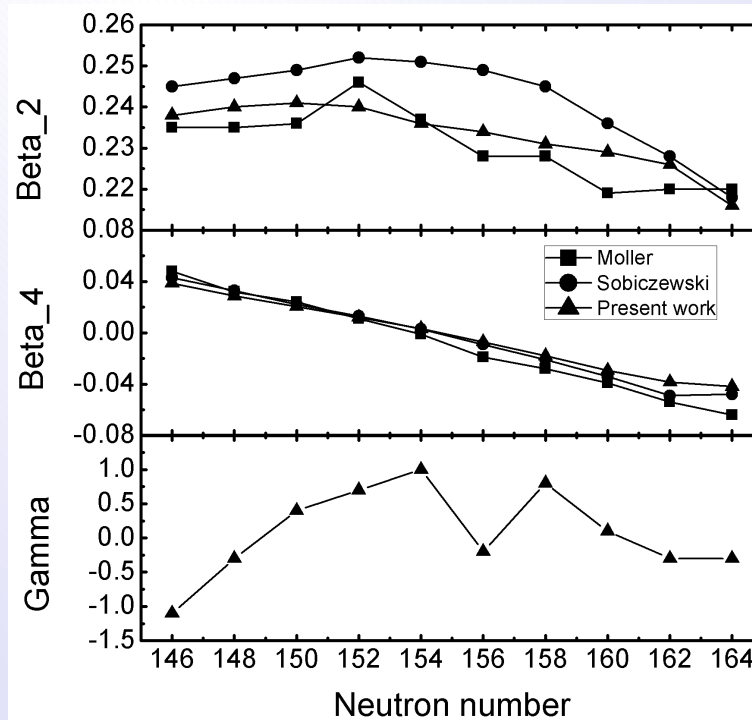
Quit

3. Results and Discussions

3.1. Ground-state properties of No isotopes



Ground-state β_2 , β_4 and γ deformations with increasing N



P. Möller et al., At Data Nucl Data Tables,59:195(1995);

A.Sobiczewski et al., PRC 63,034306(2001).



Introduction
Theoretical method
Results and...
Summary

Home Page

Title Page

Navigation arrows

Navigation arrows

Page 8 of 19

Go Back

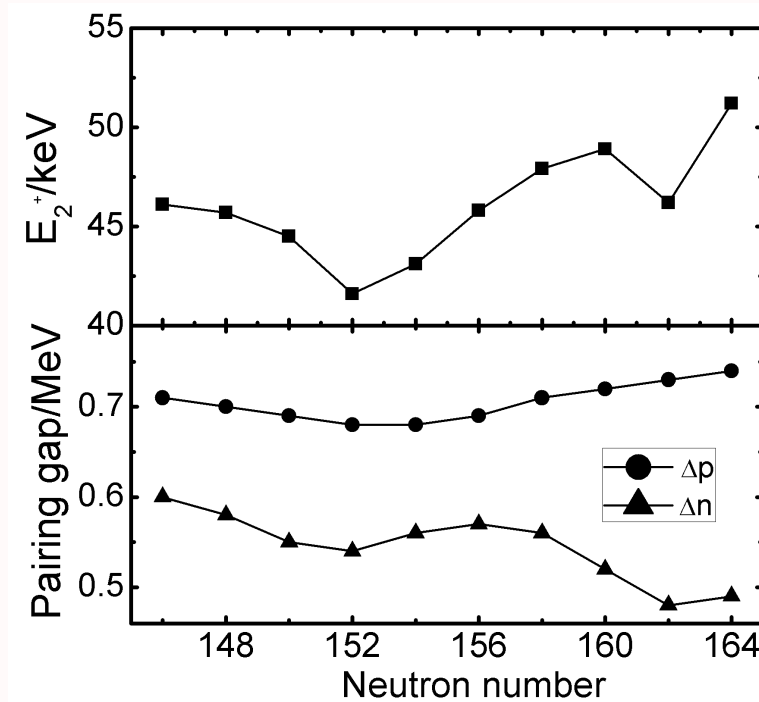
Full Screen

Close

Quit



Dependence of the energy E_{2^+} and pairing gaps on neutron number



The numbers of $N = 152$ and 162 are suggested to be shell closures.

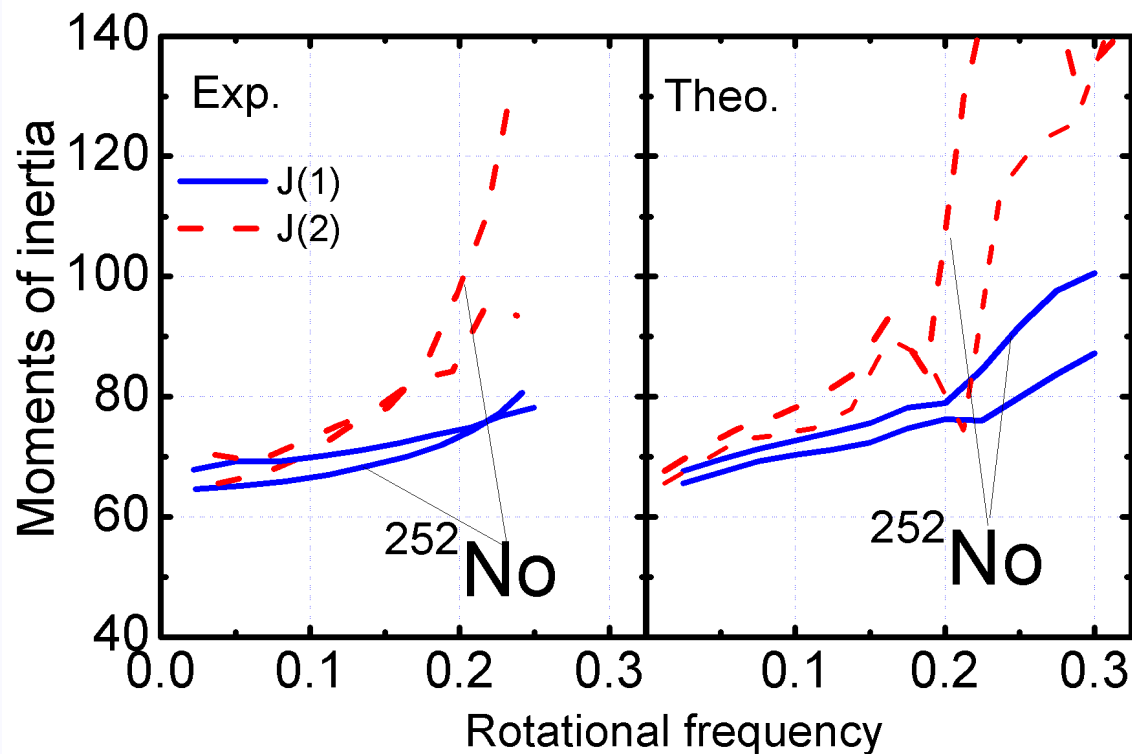
The 2^+ -state data are taken from: A.Sobiczewski et al., PRC 63,034306(2001).



3.2. High-spin properties of No isotopes



Kinematic and dynamic moments of inertia for $^{252,254}\text{No}$



Refs: R.D.Herzberg et al., PRC65,014303(2001);S.Eeckhaudt et al., EPJA26,227(2005)



Introduction
Theoretical method
Results and...
Summary

Home Page

Title Page

◀ ▶

◀ ▶

Page 10 of 19

Go Back

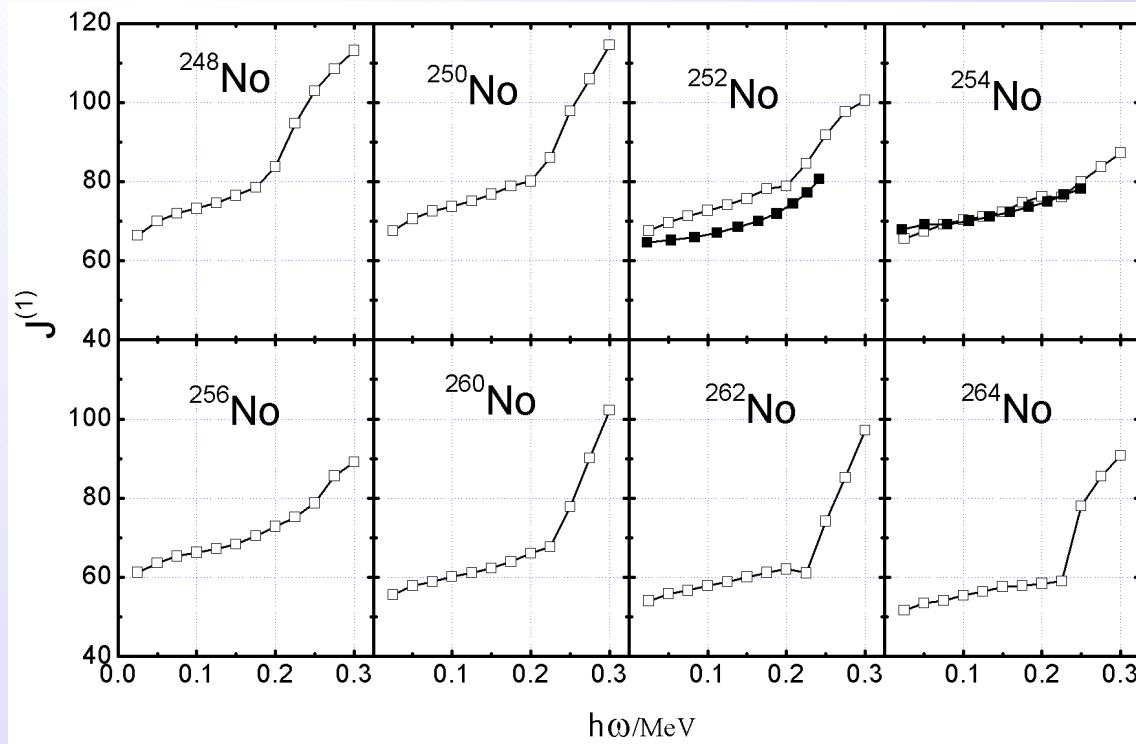
Full Screen

Close

Quit



Calculated kinematic moments of inertia for $^{248-264}\text{No}$

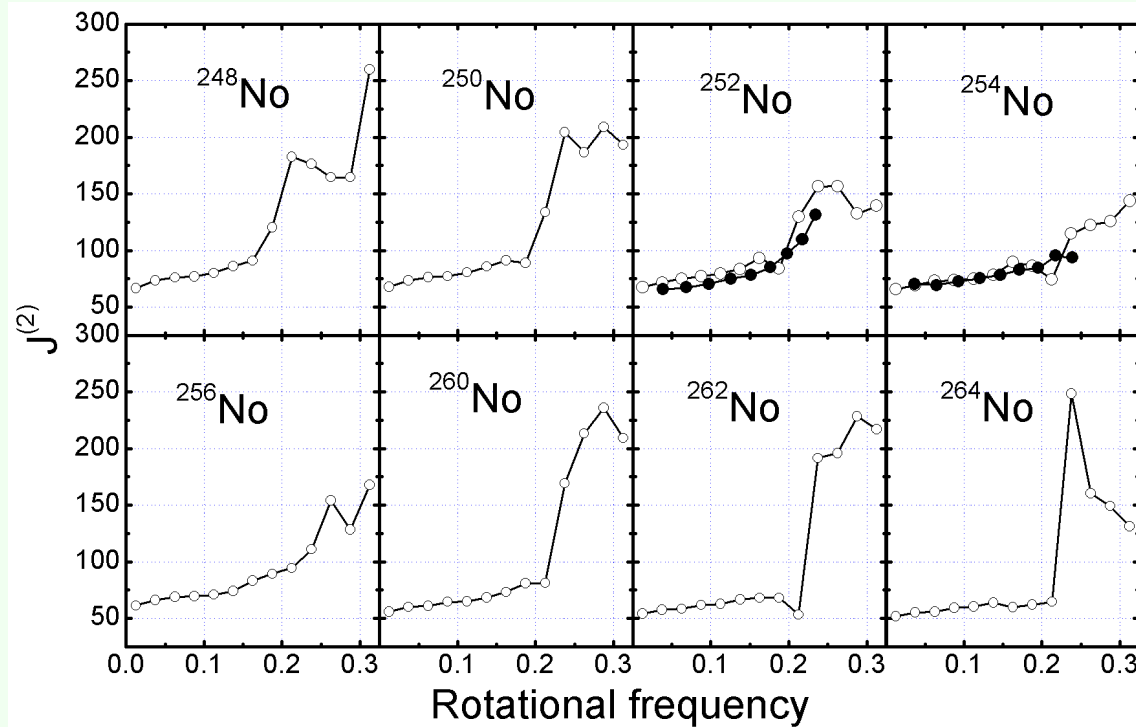


- ♣ The kinematic moments of inertia increase slowly at low spins and increase rapidly after a critical (band-crossing) spin.
- ♣ In general, this changing behavior of the moments of inertia is related to deformations and pairing correlations.





Calculated dynamic moments of inertia for $^{248-264}\text{No}$

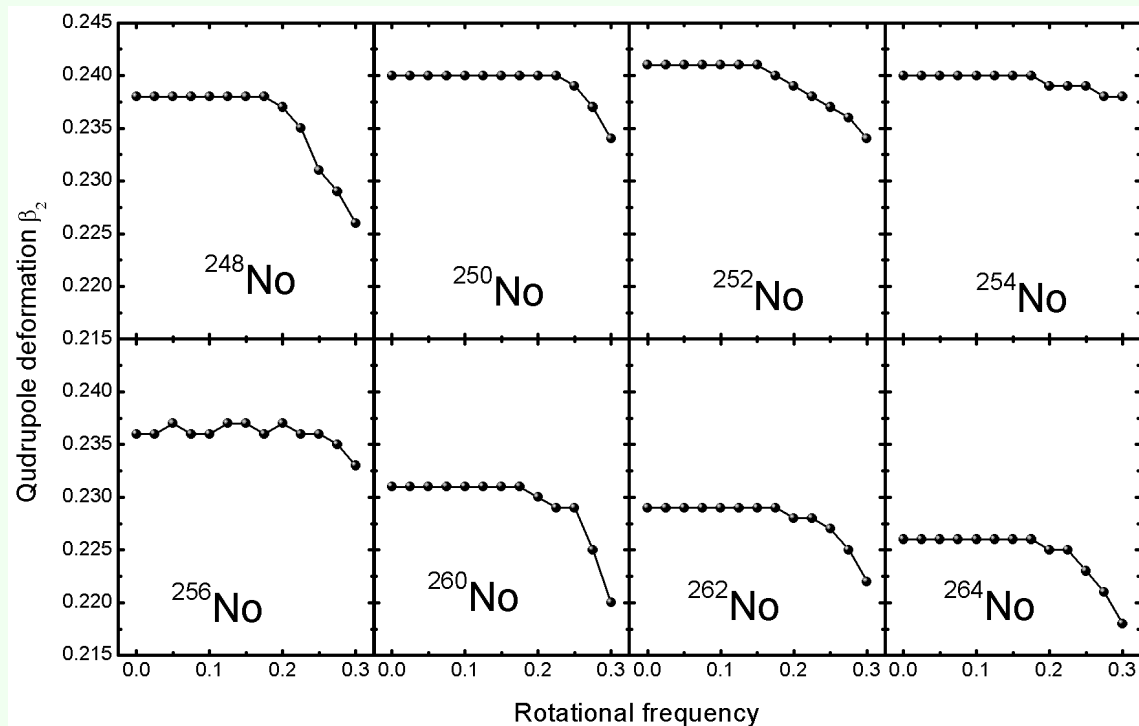


- ♣ The step increase of the dynamic moment of inertia can be explained by a band crossing of the $\pi i_{13/2}$ or $\nu j_{15/2}$ two-quasiparticle band with the zero-quasiparticle band.





Evolutions of β_2 deformations under rotation



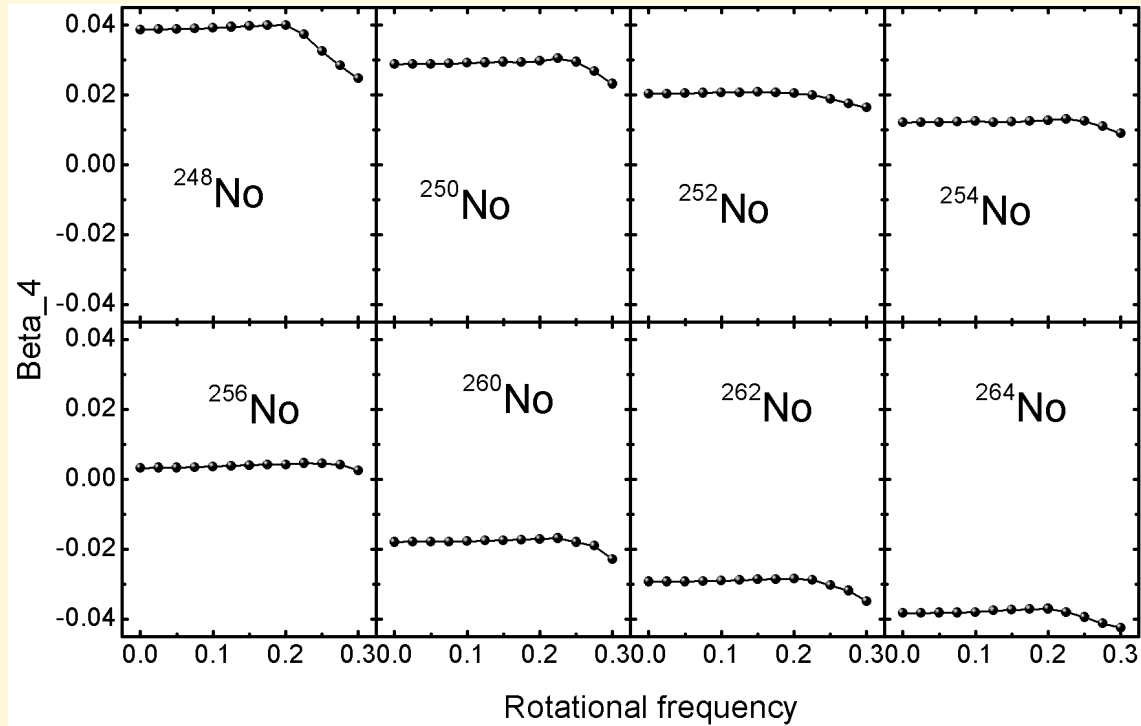
♠ β_2 maintains a constant value at low spins and decreases after a critical spin.

♠ The increasing moments of inertia with spin can not be explained by the behavior of decreasing β_2 deformations under rotation.





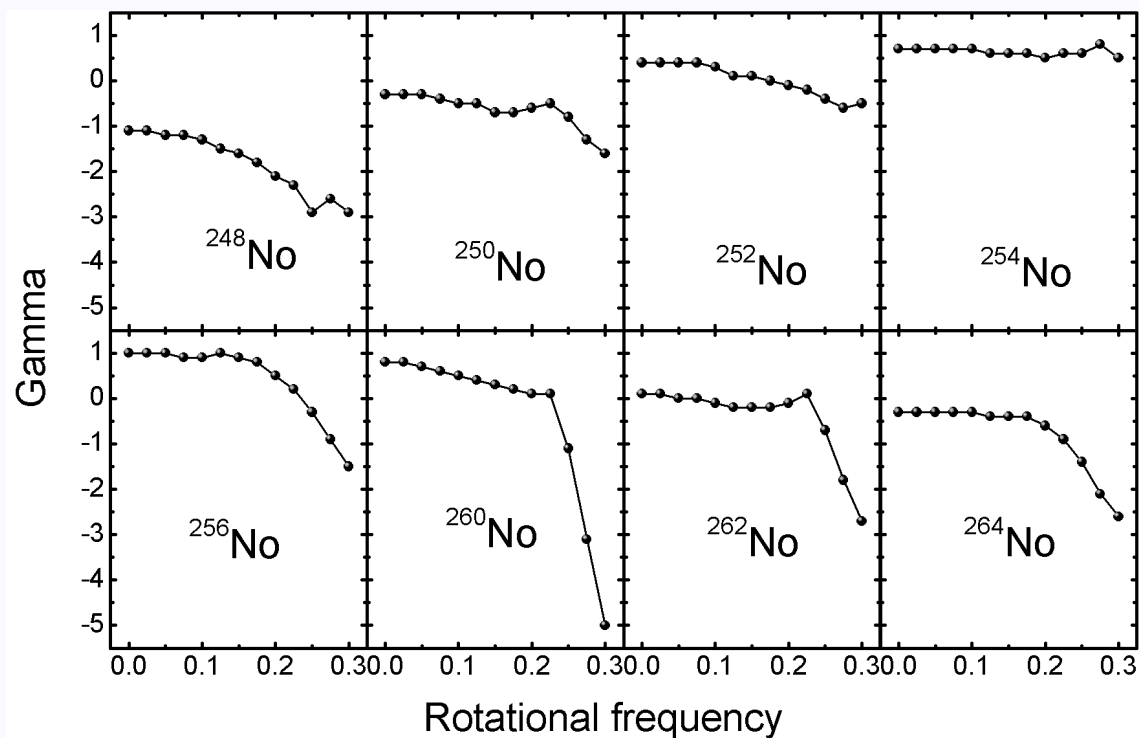
Evolutions of β_4 deformations under rotation



♠ β_4 maintains a constant value at low spins and decreases after a critical spin.



Evolutions of γ deformations under rotation



♠ With increasing rotational frequency, there is a trend that γ deformations change from positive to negative values;

♠ Very recently, Liu et al find that high-order deformation β_6 plays an important role, especially, around $N=152$. (H.L Liu et al., PRC 86,011301(2012).)



Introduction
Theoretical method
Results and...
Summary

Home Page

Title Page

◀ ▶

◀ ▶

Page 15 of 19

Go Back

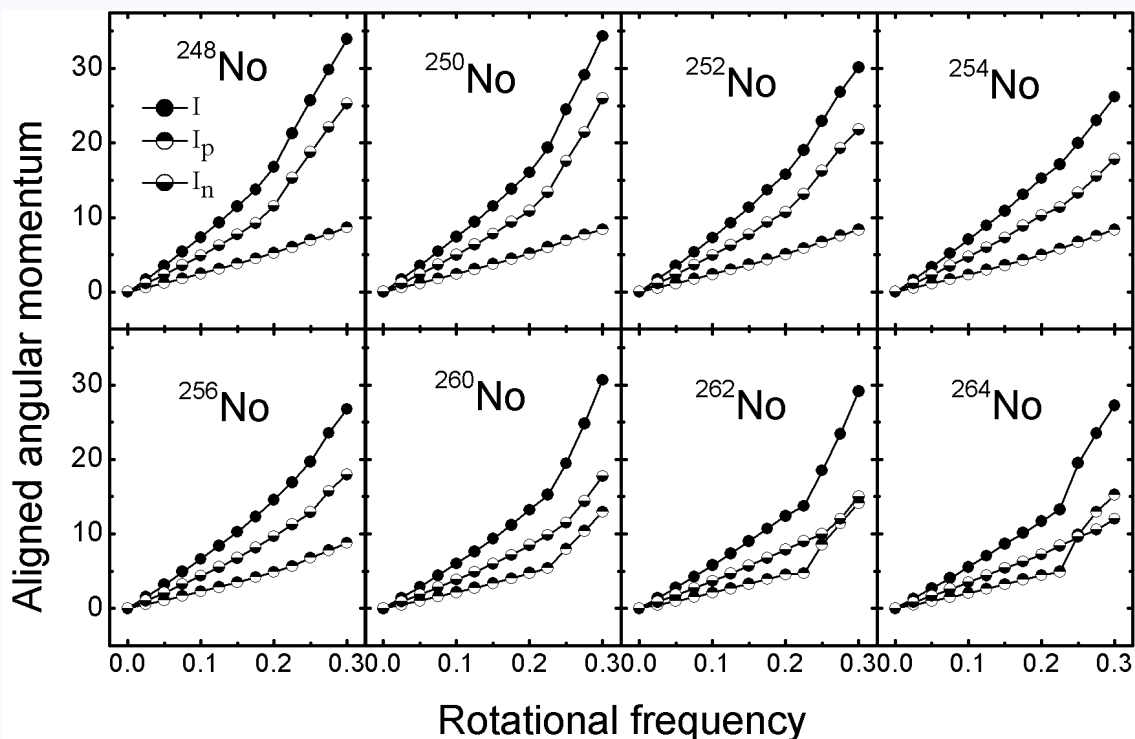
Full Screen

Close

Quit



Aligned angular momentum under rotation

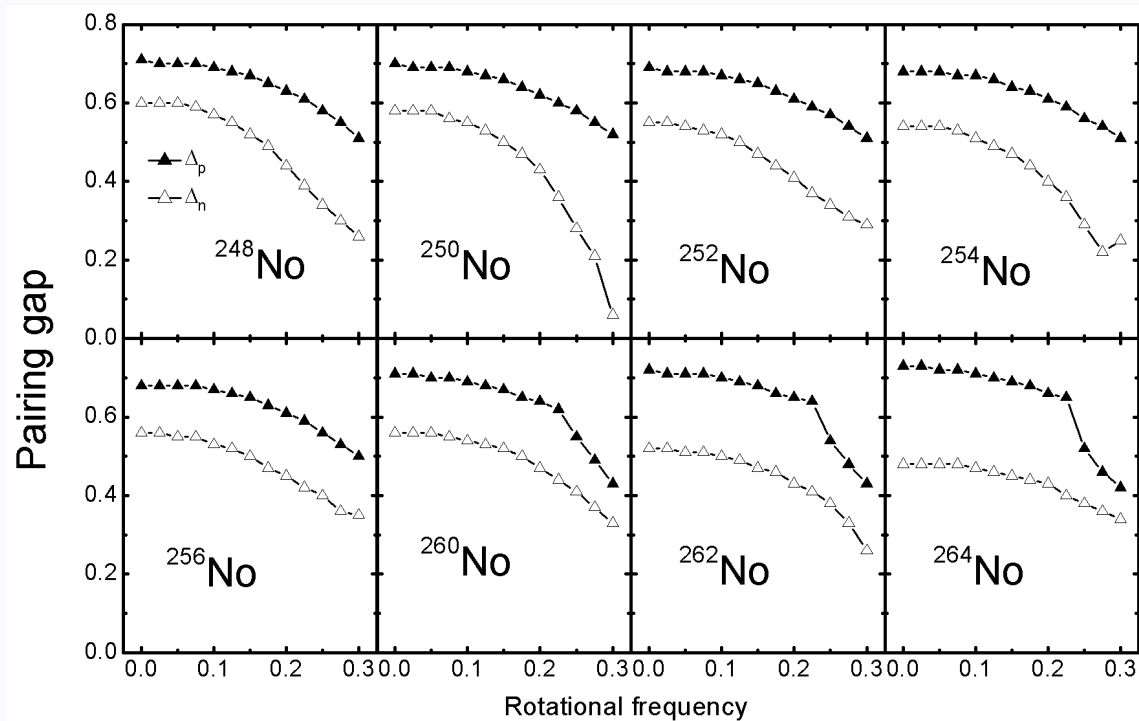


- ♠ The aligned angular momentum increases with rotational frequency, and the neutron component increases more rapidly.
- ♠ After a critical (band-crossing) point, the aligned angular momentum changes quickly. The competition of neutron and proton alignments can be seen.





Pairing gap of No isotopes under rotation



♠ The pairing energy gap for proton is larger than that for neutron.

♠ The pairing energy gap decreases with increasing rotational frequency, which may result in the decrease of MOI with spins.



Introduction
Theoretical method
Results and...
Summary

Home Page

Title Page

◀ ▶

◀ ▶

Page 17 of 19

Go Back

Full Screen

Close

Quit



4. Summary

§ Ground-state and rotational properties in No isotopes have been investigated using TRS calculations.

§ To some extent, the observed alignments in $^{252,254}\text{No}$ nuclei are reproduced.

§ The variations of moments of inertia, deformations, aligned angular momentum and pairing energy gap have been analyzed as functions of mass and rotational frequency.

§ This work provides a systematic investigation on superheavy No isotopes synthesized and a test of the present model.

Home Page

Title Page

◀ ▶

◀ ▶

Page 18 of 19

Go Back

Full Screen

Close

Quit



Introduction
Theoretical method
Results and ...
Summary

Home Page

Title Page



Page 19 of 19

Go Back

Full Screen

Close

Quit